

Factoring Trinomials

If a trinomial $ax^2 + bx + c$ will not factor by any other method, use trial and error to fit it into the F O I L pattern:

$$(a_1x + c_1)(a_2x + c_2) = (a_1a_2)x^2 + (a_1c_2 + c_1a_2)x + (c_1c_2)$$

where $a_1a_2 = a$, $a_1c_2 + c_1a_2 = b$, and $c_1c_2 = c$.

1. Set up empty parentheses: ()().
2. If a,b,c are positive, then both signs are positive (+)(+).
If b is negative but c is positive, then both signs are negative (-)(-).
If c is negative, then one sign is positive and the other is negative (+)(-).
3. Try the factors of a in front positions (a₁)(a₂), and the factors of c in the back positions (c₁)(c₂), until the resulting product is the original trinomial.

Example: factor $2x^2 - x - 10$

step 1: ()()

step 2: (+)(-)

step 3: *The factors of 2 are 2 and 1; the factors of 10 are 10 and 1 or 5 and 2:*

$$(2x + 10)(x - 1) = 2x^2 + 8x - 10$$

$$(2x + 5)(x - 2) = 2x^2 + x - 10$$

The second trial is almost correct; only the sign of the middle term is wrong. So we change signs:

$$(2x - 5)(x + 2) = 2x^2 - x - 10$$

The answer is

$$(2x - 5)(x + 2)$$