

FACTORIZING PATTERNS

$$A^2 + 2AB + B^2 = (A + B)^2$$

$$A^2 - 2AB + B^2 = (A - B)^2$$

$$A^2 + B^2 = A^2 + B^2 \text{ prime}$$

$$A^2 - B^2 = (A - B)(A + B) \text{ difference of two squares}$$

$$A^3 + B^3 = (A + B)(A^2 - AB + B^2) \text{ sum of two cubes}$$

$$A^3 - B^3 = (A - B)(A^2 + AB + B^2) \text{ difference of two cubes}$$

Geometric Representation of SUM and DIFFERENCE of CUBE patterns:

$$(\heartsuit^3 + \blacksquare^3) = (\heartsuit + \blacksquare) (\heartsuit^2 - \heartsuit\blacksquare + \blacksquare^2)$$

$$(\heartsuit^3 - \blacksquare^3) = (\heartsuit - \blacksquare) (\heartsuit^2 + \heartsuit\blacksquare + \blacksquare^2)$$

EXAMPLES:

$$\begin{aligned} (2x)^3 + y^3 &= [(2x) + y] [(2x)^2 - 2xy + y^2] \\ &= (2x + y) (4x^2 - 2xy + y^2) \end{aligned}$$

$$121 - R^2 = (11 - R) (11 + R)$$

$$27A^3 - 8B^3 =$$

$$\begin{aligned} (3A)^3 - (2B)^3 &= [3A - 2B] [(3A)^2 + (3A)(2B) + (2B)^2] \\ &= (3A - 2B) (9A^2 + 6AB + 4B^2) \end{aligned}$$

$$36X^2 + Y^2 = \text{PRIME}$$