

Derivatives

constant $\partial/\partial x (c) = 0$ where c is a constant

sum $\partial/\partial x (\mathbf{u} + \mathbf{v}) = \partial\mathbf{u}/\partial x + \partial\mathbf{v}/\partial x$

difference $\partial/\partial x (\mathbf{u} - \mathbf{v}) = \partial\mathbf{u}/\partial x - \partial\mathbf{v}/\partial x$

product $\partial/\partial x (\mathbf{u} \times \mathbf{v}) = \mathbf{u} \partial\mathbf{v}/\partial x + \mathbf{v} \partial\mathbf{u}/\partial x$

quotient $\partial/\partial x (\mathbf{u} / \mathbf{v}) = (\mathbf{v} \partial\mathbf{u}/\partial x - \mathbf{u} \partial\mathbf{v}/\partial x) / \mathbf{v}^2$

reciprocal $\partial/\partial x (1 / \mathbf{g}(x)) = - \partial/\partial x (\mathbf{g}(x)) / (\mathbf{g}(x))^2$

power rule $\partial/\partial x (\mathbf{u}^n) = n \mathbf{u}^{n-1} \partial\mathbf{u}/\partial x$ also $\partial/\partial x (\mathbf{g}(x))^n = n [\mathbf{g}(x)]^{n-1} \partial/\partial x \mathbf{g}(x)$

exponential $\partial/\partial x e^{\mathbf{u}} = e^{\mathbf{u}} \partial\mathbf{u}/\partial x$ particular case of the power rule

chain rule $\partial y/\partial x = \partial y/\partial \mathbf{u} \times \partial\mathbf{u}/\partial x = f'(\mathbf{u}) \mathbf{g}'(\mathbf{u}) = f'(\mathbf{g}(x)) \mathbf{g}'(x)$

composition $\partial/\partial x (\mathbf{f}(\mathbf{g}(x))) = f'(\mathbf{g}(x)) \mathbf{g}'(x)$

$\partial/\partial x (a^{\mathbf{u}}) = a^{\mathbf{u}} \ln a \partial\mathbf{u}/\partial x$

composition $\partial/\partial x (\mathbf{f}(\mathbf{g}(x))) = f'(\mathbf{g}(x)) \mathbf{g}'(x)$

$\partial/\partial x (a^{\mathbf{u}}) = a^{\mathbf{u}} \ln a \partial\mathbf{u}/\partial x$

$\partial/\partial x (\ln | \mathbf{u} |) = 1/\mathbf{u} \partial\mathbf{u}/\partial x$

$\partial/\partial x (\log_a | \mathbf{u} |) = 1/(\mathbf{u} \ln a) \partial\mathbf{u}/\partial x$

Derivatives of trigonometric functions:

$\partial/\partial x \sin \mathbf{u} = \cos \mathbf{u}$

$\partial/\partial x \cos \mathbf{u} = - \sin \mathbf{u} \times \partial\mathbf{u}/\partial x$

$\partial/\partial x \tan \mathbf{u} = \sec^2 \mathbf{u} \partial\mathbf{u}/\partial x$

$\partial/\partial x \cot \mathbf{u} = - \csc \mathbf{u} \times \partial\mathbf{u}/\partial x$

$\partial/\partial x \sec \mathbf{u} = \sec \mathbf{u} \tan \mathbf{u} \partial\mathbf{u}/\partial x$

$\partial/\partial x \csc \mathbf{u} = - \csc \mathbf{u} \cot \mathbf{u} \partial\mathbf{u}/\partial x$